



RESEARCH ARTICLE

Behavior of High Strength Hybrid Reinforced Concrete Deep Beams under Monotonic and Repeated Loading

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Abstract:**Introduction:**

This study presents the experimental and analytical investigation of the behavior of high strength hybrid reinforced concrete deep beams under monotonic and repeated two-point load. The idea of hybrid in this work is different. Two types of concrete were used in beam but not in cross-section. The first type was the Fibrous High Strength Concrete (FHSC) at shear spans for enhancing shear capacity against cracking due to diagonal strut failure (by adding Steel Fiber (SF) in that regions), while the second type was the Conventional High Strength Concrete (CHSC) at the mid-portion between the two strengthened shear spans.

Methods:

The experimental work included the casting and testing of ten deep beams. Five among the beams were tested under monotonic loading (control beams) and other beams were tested under repeated loading at the level of 75% of ultimate load of control beams. The effect of some selected parameters as the type of load, the hybrid and non-hybrid beams, the compressive strength of concrete (f_c) (normal and high) and the amount of web reinforcement (ρ_w) were studied in terms of crack patterns, ultimate load and load versus midspan deflection.

Results and Conclusion:

From the experimental test results, when beam cast with fibrous with SF of 1% concrete along entire length, the ultimate load of 10.96% increased as compared with hybrid beam. And it was observed to increase as much as 32.78% as compared with beam cast from conventional high strength concrete under monotonic loading. Under repeated loading of 75% control ultimate load, the ultimate load for beam cast with fibrous concrete along entire length increased as much as 15.32% as compared with hybrid beam. And it was seen to increase 36.17% as compared with the beam cast from conventional high strength concrete. The percentage increase in ultimate load of hybrid (SF ratio 1%) deep beam cast with high strength concrete became 97.3% as compared with the identical beam cast with normal strength concrete under monotonic loading and (98.21%) under repeated loading (load 75% control beam load). The percentage increase as ultimate load for hybrid beam cast with SF ratio 1% was 9.62% as compared with hybrid beam with SF ratio 0%. As the web reinforcement increased from 0 to 0.004 and from 0 to 0.006, the percentage increased in the ultimate load as 28.07% and 57.89%, under monotonic loading as 26.14% and 59.09%, under repeated loading.

Then, Strut and Tie model (STM) procedures were used to analyze the experimentally tested hybrid deep beams under monotonic loading of the present investigation. Comparison of experimental results was made with corresponding predicted values using the STM procedure presented of ACI 318R-14 Code and with other procedures

Keywords: High strength, Deep beam, Hybrid, Fibrous high strength concrete, Conventional concrete, Strut and Tie model.

1. INTRODUCTION

The deep beam could be defined as associate load on the face and the inversion face. The compression elements can

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expand among the support and loads under ACI-Code 318R-14. The clear span and total depth ratio of less than four and the shear span to depth ratio of less than two [1]. There are many applications for reinforced concrete deep beams such as buildings, bridges, offshore structures and foundations. There are many structural elements which behave as a deep beam such as transfer beams, load-bearing walls and coupling beams in buildings, pile caps in foundations, plate elements in the folded plates and bunker walls [2]. Beams, in general, are classified as shallow beams, moderate deep beams, and deep beams according to their span to depth ratios. Beams whose depths are comparable to their spans may be described as deep beams. There is a distinct change in the behavior of deep beams and moderate deep beams because of the presence of local lateral normal forces in addition to usual bending moments and shear forces. This is not true for shallow beams. There is a gradual transition from shallow beam behavior to deep beam behavior. In construction, deep beams are widely used in water tanks, underground bunkers, silos, nuclear reactors, where walls act as vertical beams spanning between column supports. Sometimes pile caps are also designed as deep beams. Deep beams and moderate deep beams occur frequently in modern buildings such as departmental stores, hotels and theatres where it is desired to have the lower floor completely free of columns. In reinforced concrete hipped plate construction, the supporting diaphragms often behave as deep beams.

2. AIM AND IDEA OF THE PRESENT STUDY

The concept of hybrid deep beams in this work is different from the other works which use more than one type of concrete in cross section. In the precast work, the layers were cast vertically in longitudinal direction but not in cross-section. The aim is to strengthen shear spans which subjected to heavy shear forces (compression struts) lead to shear failure. Strengthen as done by adding steel fibers with different ratios to those spans increase their tensile strength. As the deep beams of the flexural members did not mention in the title 'the calculation of the shear force' because the main problem in this type of beam is the shear force and this was observed in the practical results. A flexural member whose span-to-depth ratio is too low to accurately apply the principles of sectional design through sectional properties and internal forces shear strength the maximum shearing stress a flexural member can support at a specific location as controlled by the combined effects of shear forces and bending moment.

3. EXPERIMENTAL WORK

A total of ten simply supported deep beams have been tested under two point loads to investigate the behavior of high strength hybrid reinforced concrete deep beams under monotonic and repeated loading. The tested beams have been designed to guarantee shear failure under monotonic loading according to ACI 318 R-14Code (STM). All beams had the same dimensions and flexural reinforcement. The amount of flexural reinforcement for all the tested beams was where is the flexural reinforcement ratio). The clear span between supports was 1230 mm which results in a ratio of clear span to generally depth of 3.5 which is less than 4.0 as recommended by the conditions of the ACI 318M-14 Code for deep beam requirements. Table 1 shows tests results of mechanical properties for hardened concrete.

Table 1. Tests results of mechanical properties for hardened concrete.

Beam Designation	Type of Beam	f'c (MPa)		ft (MPa)		fr (MPa)		Ec (GPa)	
		HSC	FHSC	HSC	FHSC	HSC	FHSC	HSC	FHSC
B -HS-M-FHSC1- ρ_w 4 B -HS-R-FHSC 1- ρ_w 4	Non-Hybrid (FHSC)	-	56	-	7.12	-	11.5	-	81
B -HS-M-Hy1- ρ_w 4 B -HS-R-Hy1- ρ_w 4	Hybrid	53.8	56	5.4	6.51	9.4	11.3	63	82.5
B - HS-M-Hy1- ρ_w 6 B -HS-R-Hy1- ρ_w 6	Hybrid	53.8	56	5.4	6.51	9.4	11.3	63	82.5
B -NC-M-Hy1- ρ_w 4 B -NC-R-Hy1- ρ_w 4	Hybrid (NSC)	27.33	29	3.54	4.75	3.5	5.5	23.5	24.7
B -HS-M-HSC 0- ρ_w 4 B -HS-R-HSC 0- ρ_w 4	Non -Hybrid (HSC)	56.4	-	5.3	-	7.5	-	62.25	-

The horizontal length of all longitudinal reinforcement 1460mm and vertical length 250mm to make 90° hook to provide sufficient anchorage as shown in Fig. (1)



Fig. (1). Steel reinforcement cage used for deep beam.

3.1. Molds

The steel molds were designed for casting four hybrid deep beams for each batch as shown in Fig. (2). The inside dimensions for each mold were 1500mm length, 350mm height and 150mm width. The molds were designed to cast the beams vertically due to the difficulty of casting layers in a horizontal state. The front cover of the mold face of dimensions 1500mm×350mm consists of three plates. The lower plate was fixed to cast the first layer while the two other plates above were movable (doors) to cast the two other layers. Each door was closed before casting the layer of beam in it.



Fig. (2). Steel molds used for casting hybrid deep beams.

3.2. Test Procedure

In order to test the beam, the faces of the samples were coated in white color for observing cracks easily. The support and load point locations were positioned and thereafter, the points were mounted on the beams. The beams were categorized and the site of support point, loading point, and the digital gage places were noticeable on the beams to ease the accurate setup of testing machine. Thereafter, the beam was elevated by electrical crane and depressed on to supports. Beam specimens were located at the testing machine and checked so that the centerline supports, load arms

and dial gages were fixed at their right and suitable positions. Loading process commences by application of two-point load from the testing machine to the higher face of beam.

All beam specimens have been loaded until failure for monotonic test and five cycles in repeated loading test. The beam samples have been loaded in increases of 10kN, the rate of load increase was around 1.5kN/sec.

The locations and expansion of cracks for each cycle were noticeable on the surface of the beam. The failure happened, while the beam failed abruptly at simultaneity with the load index stopped in record or reoccurrence back and the deflection increased very quickly. The ultimate load has been noted, and the load has been removed to permit taking some photographs of the crack pattern and the mode of failure.

4. EXPERIMENTAL RESULTS

In monotonic loading, at low load levels, all the tested beams behaved in an elastic manner and the deflections at mid-span are small and proportional to the applied load. The first diagonal crack (web shear crack) appears at the diagonal region bounded by load and supports positions towards or parallel to the line joining the support with the load. The first flexure crack is observed in the lower part of the beam at the middle region between load positions. In repeated loading, at the first cycle, the behavior of deep beam specimens was similar to the behavior of beams under monotonic loading until the load reached the required load level. The cracks were opened during the first cycle as the required load level was reached, then closed at the unloading part of the cycle. Failure occurs by splitting the beam into two parts approximately along the line connecting the edge steel blocks at the support expect B-HS-M-Hy 1- ρ_w 6 failed in flexural (crushing compression chord). Details of the tested beams and results obtained are shown in Table 2.

Table 2. Summary of test results for tested deep beams*.

Beam Designation	Type of Beam	f'c	ρ_w **	SF (%)	Type of Loading	No. of Cycles	Pu (kN)	Mode of Failure
B -HS-M-FHSC 1- ρ_w 4	Non-Hybrid (FHSC)	60	0.004*** (Min)	1	Monotonic	-	810	Diagonal Shear Failure
B -HS-R-FHSC 1- ρ_w 4	Non-Hybrid (FHSC)	60	0.004 (Min)	1	Repeated (75% of Ultimate Load for Last Beam)	5	640	Diagonal Shear Failure
B -HS-M-Hy1- ρ_w 4	Hybrid	60	0.004 (Min)	1	Monotonic	-	730	Diagonal Shear Failure
B -HS-R-Hy1- ρ_w 4	Hybrid	60	0.004 (Min)	1	Repeated (75% of Ultimate Load for Last Beam)	5	555	Diagonal Shear Failure
B -HS-M-Hy1- ρ_w 6	Hybrid	60	0.006 (>Min)	1	Monotonic	-	900	Diagonal Shear Failure
B -HS-R-Hy1- ρ_w 6	Hybrid	60	0.006 (>Min)	1	Repeated (75% of Ultimate Load for Last Beam)	5	700	Shear-Flexural Failure
B -NC-M-Hy1- ρ_w 4	Hybrid	30	0.004 (Min)	1	Monotonic	-	370	Diagonal Shear Failure
B -NC-R-Hy1- ρ_w 4	Hybrid	30	0.004 (Min)	1	Repeated (75% of Ultimate Load for Last Beam)	5	280	Diagonal Shear Failure
B -HS-M-HSC 0- ρ_w 4	Non-Hybrid (HSC)	60	0.004 (Min)	0	Monotonic	-	610	Diagonal Shear Failure
B -HS-R-HSC 0- ρ_w 4	Non-Hybrid (HSC)	60	0.004 (Min)	0	Repeated (75% of Ultimate Load for Last Beam)	5	470	Diagonal Shear Failure

*All beams have the same (a/h) ratio = 1.14.

Figs. (3a-j) shows mode of failure and the crack pattern of the tested deep beams after testing.

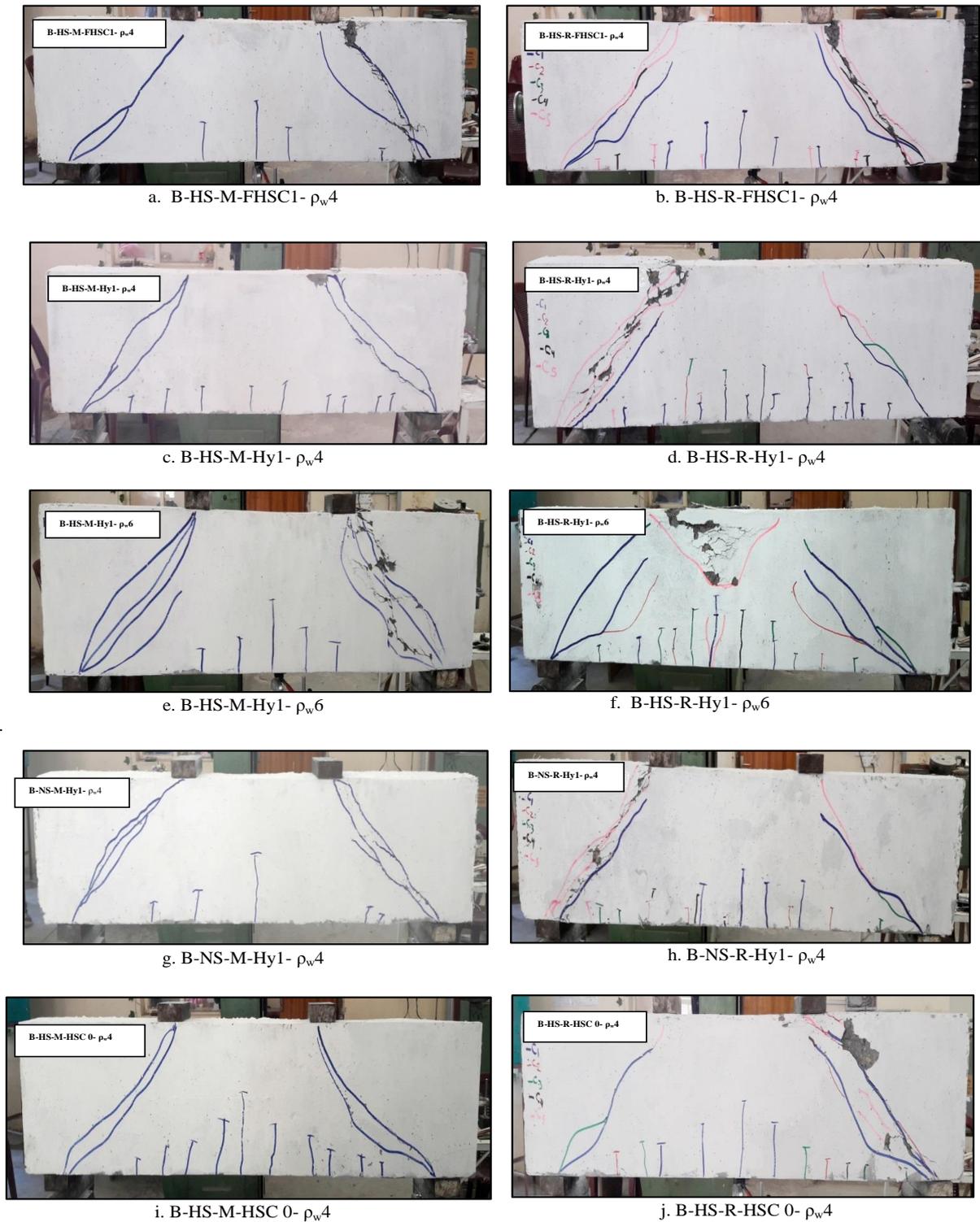


Fig. (3). Mode of failure and the crack pattern of the tested deep beams.

4.1. Effect of Many Parameters on the Ultimate Load of Tested Beams

Type of loading in deep beams monotonic and repeated with load level 75% from monotonic. Table 3 explains the effect type of loading on the ultimate load.

4.1.1. Effect Type of Loading

Table 3. Effect of loading type for all tested deep beam.

Beam Designation	Type of Beam	f'c	ρ_w	SF (%)	Type of Loading	No. of Cycle	Pu (kN)	% Percentage Decrease
B -HS-M-FHSC 1- ρ_w 4	Non-Hybrid (FHSC)	60	0.004	1	Monotonic (Control)	-	810	20.98
B -HS-R-FHSC 1- ρ_w 4	Non-Hybrid (FHSC)	60	0.004	1	Repeated(75% of Control Beam Load)	5	640	
B -HS-M-Hy1- ρ_w 4	Hybrid	60	0.004	1	Monotonic (Control)	-	730	23.97
B -HS-R-Hy1- ρ_w 4	Hybrid	60	0.004	1	Repeated(75% of Control Beam Load)	5	555	
B -HS-M-Hy1- ρ_w 6	Hybrid	60	0.006	1	Monotonic (Control)	-	900	22.22
B -HS-R-Hy1- ρ_w 6	Hybrid	60	0.006	1	Repeated(75% of Control Beam Load)	5	700	
B -NC-M-Hy1- ρ_w 4	Hybrid	30	0.004	1	Monotonic (Control)	-	370	24.32
B -NC-R-Hy1- ρ_w 4	Hybrid	30	0.004	1	Repeated(75% of Control Beam Load)	5	280	
B -HS-M-HSC 0- ρ_w 4	Non-Hybrid (HSC)	60	0.004	0	Monotonic (Control)	-	610	22.95
B -HS-R-HSC 0- ρ_w 4	Non-Hybrid (HSC)	60	0.004	0	Repeated(75% of Control Beam Load)	5	470	

X' = 22.89

From the observation of Table 3, the following notes can be noticed:

1. The decreased percentages in the ultimate load according to the repeated loading for non-hybrid deep beams of HSC and FHSC are convergent which are 22.95% and 20.98%, respectively.
2. The decreased percentages in the ultimate load according to the repeated loading of hybrid deep beams which have web reinforcement (0.004 and 0.006) as variable are convergent which are 23.97% and 22.22%, respectively.
3. The decreased percentages in the ultimate load according to the repeated loading of hybrid deep beams with compressive strength concrete (high and normal) as variable are convergent which are 23.97% and 24.32%, respectively.
4. The average value of the decreased percentages of beams subjected to monotonic and 75% of the repeated loading is 22.88%.

4.2. Effect Compressive Strength of Concrete

4.2.1. Under Monotonic Loading

Fig. (4) and Table 4 shows the effect of the compressive strength of concrete on the ultimate loads for deep beams which were tested under monotonic loading. About 30MPa and 60MPa.

Table 4. Effect of the compressive strength of concrete on ultimate load of beams under monotonic loading.

Beam Designation	Type of Beam	SF (%)	ρ_w	Ultimate Load (Pu) (kN)	% Increase Ultimate Load *
B-NS-M-Hy1- ρ_w 4	Hybrid(NS)	1	0.004	370	-
B-HS-M-Hy1- ρ_w 4	Hybrid(HS)	1	0.004	730	97.3

*The percentage increase is measured with respect to beam B-NS-M-Hy1 ρ_w 4 .

The results in Table 4 show the increase in ultimate load in hybrid deep beams tested under monotonic load beam

B-HS-M-Hy1- ρ_w 4 is 97.3% as compared with beam B-NC-M-Hy1- ρ_w 4. It can be observed that as the compressive strength increases, the capacity increased which is an expected result.

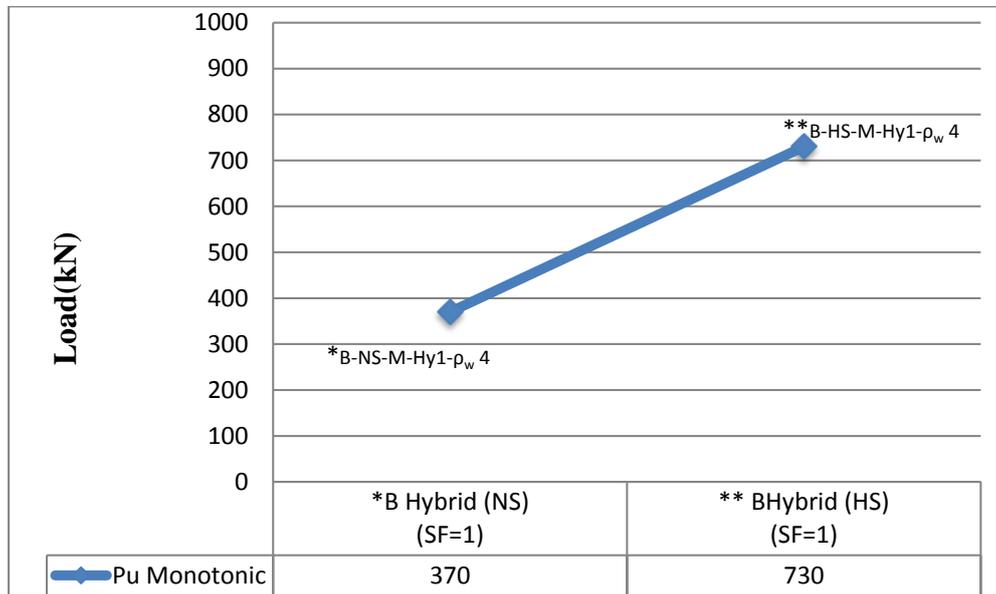


Fig. (4). Effect compressive strength of concrete on ultimate load of beams under monotonic loading.

4.2.2. Under Repeated Loading

Fig. (5) and Table 5 shows the effect of strength of concrete (as 30 MPa and 60 MPa) on an ultimate load of hybrid deep beam tested under repeated loading level of 75% of control monotonic loading.

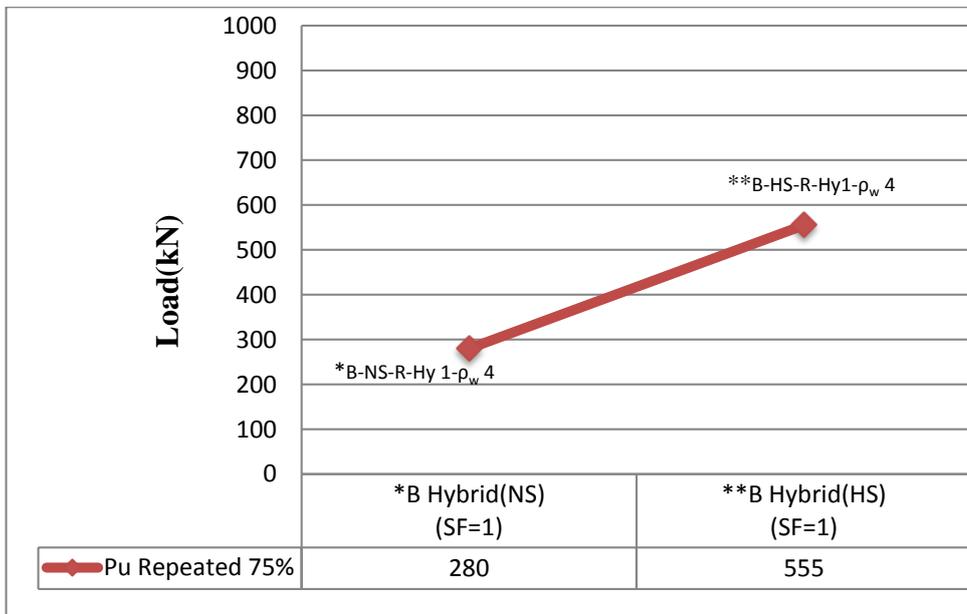


Fig. (5). Effect of compressive strength of concrete on ultimate load of beams under repeated loading.

Table 5. Effect type of beam on ultimate load under monotonic loading.

Beam Designation	Type of Beam	SF (%)	ρ_w	Ultimate Load (Pu) (kN)	%Increase Ultimate Load*
B-NS-R-Hy1- ρ_w 4	Hybrid (NC)	1	0.004	280	-
B-HS-R-Hy1- ρ_w 4	Hybrid (HS)	1	0.004	555	98.21

*The percentage of increase is measured with respect to beam B-NS-R-Hy1- ρ_w 4.

From the results in Table 5, it can be seen that hybrid beams tested under repeated loading with higher compressive strength have a higher ultimate load. The percentage increases ultimate load, hybrid beam B-HS-R-Hy1- ρ_w 4. From Tables 4 and 5, it can be seen that in both types of loading (repeated and monotonic), the ultimate load is doubled as the compressive strength increased from 28.17MPa to 55MPa.

4.3. Effect Type of Beam

4.3.1. Under Monotonic Loading

Effects of the variable type of beam on the ultimate load for deep beams tested under monotonic load in this research are shown in Fig. (6) and Table 6. Beam B-HS-M-HSC 0- ρ_w 4 was cast using HSC, beam B-HS-M-FHSC1- ρ_w 4 was cast using FHSC and beam B-HS-M-Hy1- ρ_w 4 was cast hybrid (HSC at mid span and FHSC at sides).

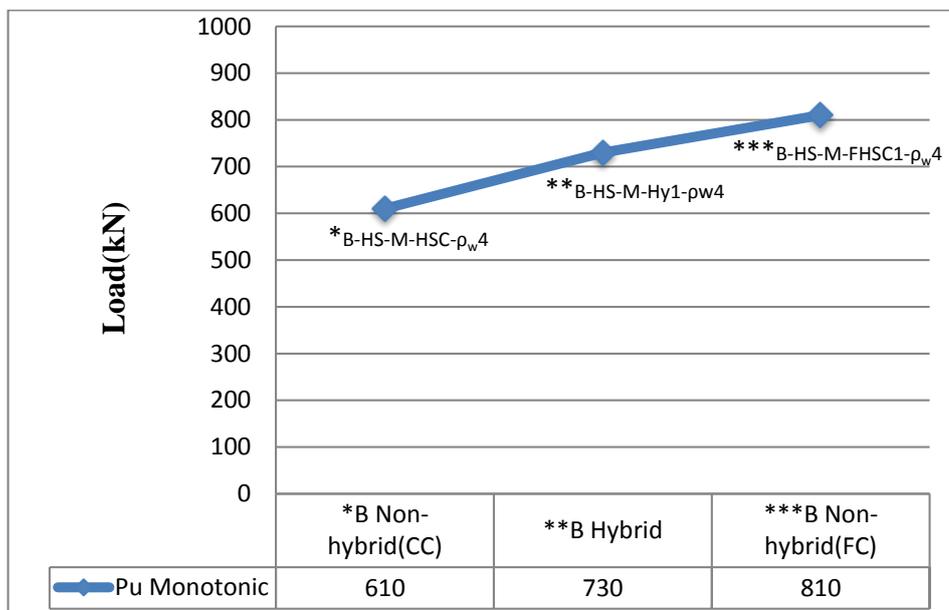


Fig. (6). Effect type of beam on ultimate load under monotonic loading.

Table 6. Effect type of beam on ultimate load under monotonic loading.

Beam Designation	Type of Beam	SF (%)	ρ_w	Ultimate Load (Pu) (kN)	% Increase Ultimate Load *
B-HS-M-HSC 0- ρ_w 4	Non -Hybrid (HSC)	0	0.004	610	-
B-HS-M-Hy1- ρ_w 4	Hybrid	1	0.004	730	19.67
B-HS-M-FHSC 1- ρ_w 4	Non-Hybrid (FHSC)	1	0.004	810	**32.79

*The percentage of increase is measured with respect to beam B-HS-M-HSC 0- ρ_w 4. ** The percentage of increase of a load of beam B-HS-M-FHSC 1- ρ_w 4 is 10.96 with respect to beam B-HS-M-Hy1- ρ_w 4.

The results presented in Table 6, show that the increase in ultimate load for beam B-HS-M-FHSC1- ρ_w 4 which cast using FHSC and beam B-HS-M-Hy1- ρ_w 4 is about 32.79% and 19.67%, respectively, with respect to beam B-HS-M-HSC 0- ρ_w 4 which cast with HSC. From this result, it is observed that the extension ratio of SF (1%) to beam B-HS-M-Hy1- ρ_w 4 in shear spans only leads to improve the amount of resistance by a significant ratio of 19.67%, while when the

same proportion of SF was extended through the length of the beam B-HS-M-FHSC1- ρ_w 4, the percent of increase is also significant 32.79% but a bit higher than the hybrid beam with SF only at shear spans 10.96%.

4.3.2. Under Repeated Loading

Fig. (7) and Table 7 shows the effect of the beam type on ultimate load for deep beams tested under repeated loading by 75% of the ultimate monotonic loading of its control beams.

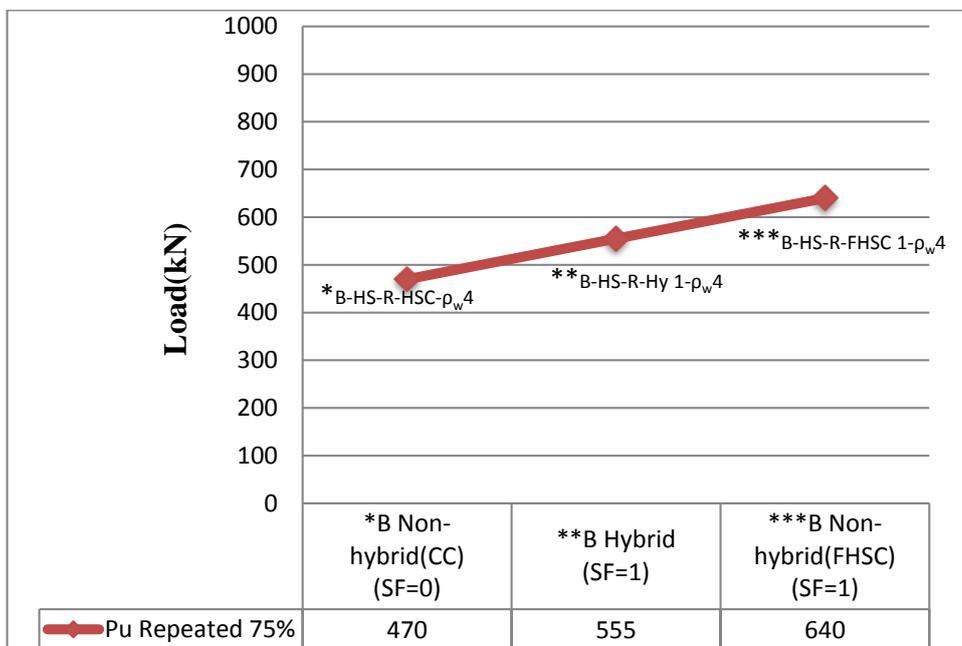


Fig. (7). Effect type of beam on ultimate load under repeated loading.

Table 7. Effect type of beam on ultimate load under repeated loading.

Beam Designation	Type of Beam	SF (%)	ρ_w	Ultimate Load (Pu) (kN)	% Increase Ultimate Load *
B-HS-R-HSC 0- ρ_w 4	Non-Hybrid (HSC)	0	0.004	470	-
B-HS-R-Hy1- ρ_w 4	Hybrid	1	0.004	555	18.09
B-HS-R-FHSC 1- ρ_w 4	Non-Hybrid (FHSC)	1	0.004	640	**36.17

*The increased percentage is measured with respect to beam B-HS-R-HSC 0%- ρ_w 4. **The percentage increase of load of beam B-HS-R-FHSC 1%- ρ_w 4 is 15.32 with respect to beam B-HS-R-Hy1%- ρ_w 4.

From the results in Table 7, it can be seen that the hybrid deep beam B-HS-R-Hy1- ρ_w 4 fails in load higher than non-hybrid deep beam cast with HSC by 18.09%, while deep beam B-HS-R-FHSC 1- ρ_w 4 which was cast from FHSC with SF ratio of 1% fails in load higher than the two beams B-HS-R-HSC 0- ρ_w 4 and B-HS-R-Hy1- ρ_w 4 by 36.17% and 15.32%, respectively. It can be concluded that the ratio of SF in the region of pure bending in beams subjected to the repeated loading level of 75% of monotonic ultimate load of like beams are more considerable when beams subjected to repeated loading than in monotonic loading.

4.4. Effect of Web Reinforcement Ratio (ρ_w)

Three arrangements of web reinforcement were considered (0,0.004,0.006). The ratio 0.004 represents minimum web reinforcement (minimum horizontal 0.0025 and minimum vertical 0.0025).

4.4.1. under Monotonic Loading

Effect of amount of web reinforcement is calculated under the constant ratio of SF and a/h ratio for two types of loading monotonic and repeated of 75% control ultimate load. The results of the variable ρ_w are shown in Fig. (8) and Table 8.

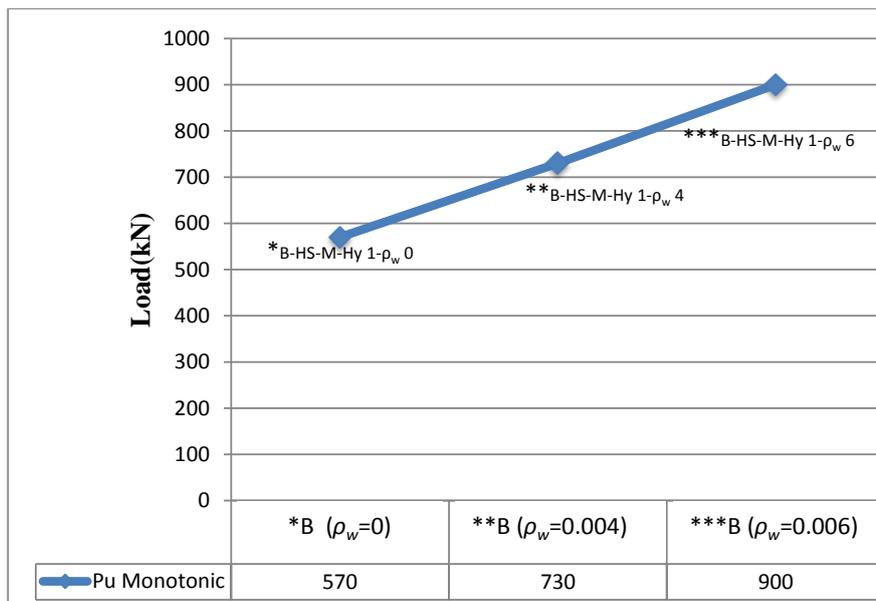


Fig. (8). Effect of ρ_w on ultimate load of beams under monotonic loading.

Table 8. Effect of ρ_w on ultimate load of beams under monotonic loading.

Beam Designation	Type of Beam	SF (%)	ρ_w	Ultimate Load (Pu) (kN)	% Increase Ultimate Load *
B-HS-M-Hy1- ρ_w 0	Hybrid	1	0.0	570	-
B-HS-M-Hy1- ρ_w 4	Hybrid	1	0.004	730	28.07
B-HS-M-Hy1- ρ_w 6	Hybrid	1	0.006	900	**57.89

* The percentage of increase is measured with respect to beam B-HS-M-Hy1- ρ_w =0.

4.4.2. Under Repeated Loading

The effect of an ultimate load for hybrid deep beams under repeated loading of level 75% of control monotonic loading is shown in Fig. (9) and Table 9.

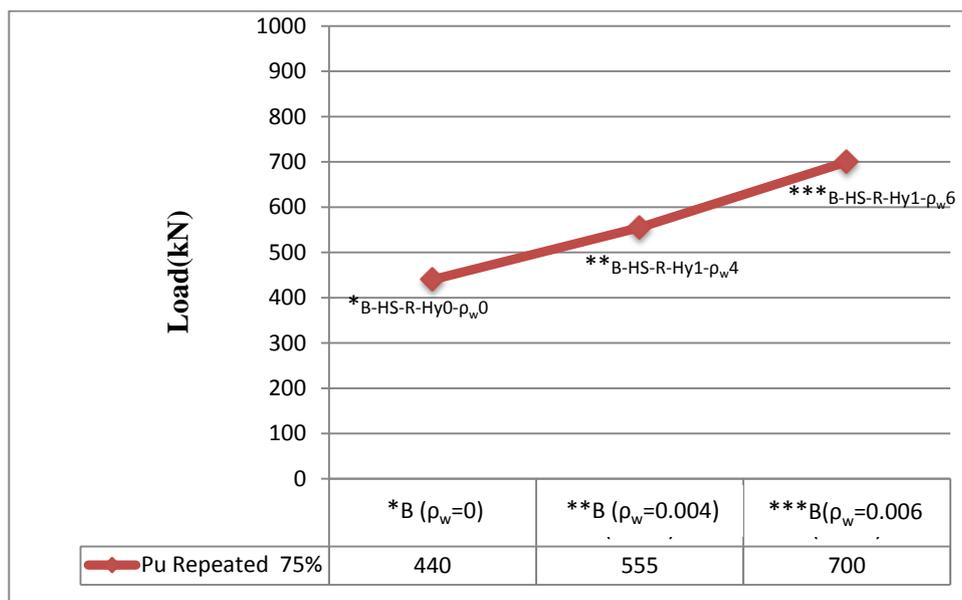


Fig. (9). Effect of ρ_w on ultimate load of beams under repeated loading.

Table 9. Effect of ρ_w on ultimate load of beams under repeated loading.

Beam Designation	Type of Beam	SF (%)	ρ_w	Ultimate Load (Pu) (kN)	% Increase Ultimate Load *
B-HS-R-Hy1- ρ_w 0	Hybrid	1	0.0	440	-
B-HS-R-Hy1- ρ_w 4	Hybrid	1	0.004	555	26.14
B-HS-R-Hy1- ρ_w 6	Hybrid	1	0.006	700	**59.09

*The percentage of increase is measured with respect to beam B-HS-R-Hy1- ρ_w =0. ** the increased percentages of load of the beam B-HS-R-Hy1- ρ_w 6 is 26.13% with respect B-HS-R-Hy1- ρ_w 4.

It can be seen that there is an increase in the value of ultimate load value of 26.14% as ρ_w increases from (0 to 0.004) while there is an increase in ultimate load value of 59.1% as the ρ_w increased from (0 to 0.006). It can be concluded that presence of web reinforcement contributes to enhance shear capacities of hybrid deep beams with significant effected under monotonic and repeated loading. Also, the increase in web reinforcement ratio from 0.004 to 0.006 increases the capacity by 26.13%.

4.5. Load-Deflection Response

4.5.1. Effect Compressive Strength of Concrete

Fig. (10) shows the effect of the compressive strength of concrete of hybrid deep beams with SF 1% on load-deflection response under monotonic loading. Two types of strength were used. Hybrid beam B-HSC-M-Hy1- ρ_w 4, with normal strength (f_c =28.17Mpa) has the smaller deflection values at each stage of loading as compared to beam B -HS-M-Hy1- ρ_w 4 that has high strength (f_c =55Mpa).

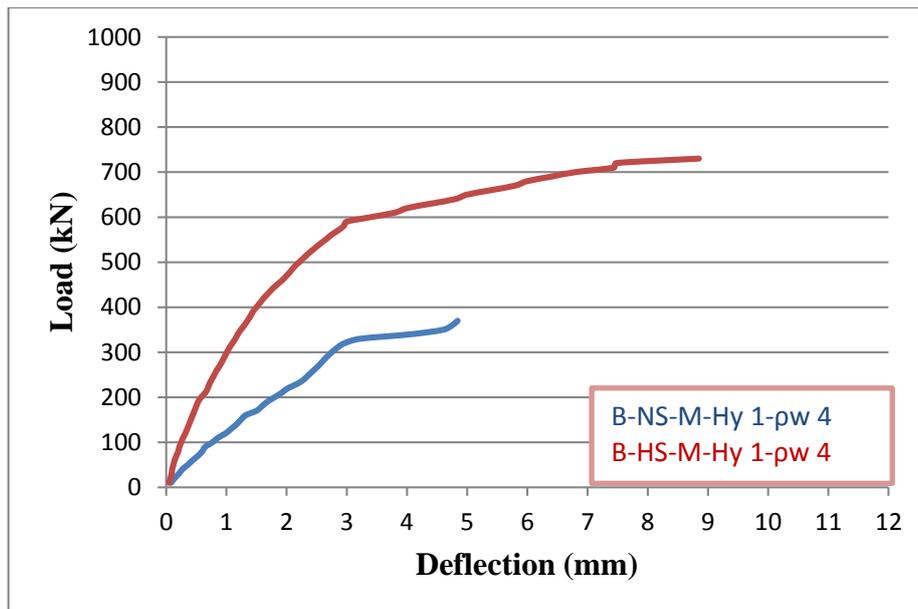


Fig. (10). Load-deflection relationship for hybrid beams with different strength of concrete under monotonic loading.

4.5.2. Effect Type of Beam

Fig. (11) shows the difference between load-deflection relationship of non-hybrid (HSC) beam B-HS-M-HSC 0- ρ_w 4, beam B-HS-M-Hy1- ρ_w 4 (hybrid beam with SF ratio 1% in shear spans) and non-hybrid (FHSC) beam B-HS-M-FHSC- ρ_w 4 with SF ratio of 1% along entire beam length under monotonic loading.

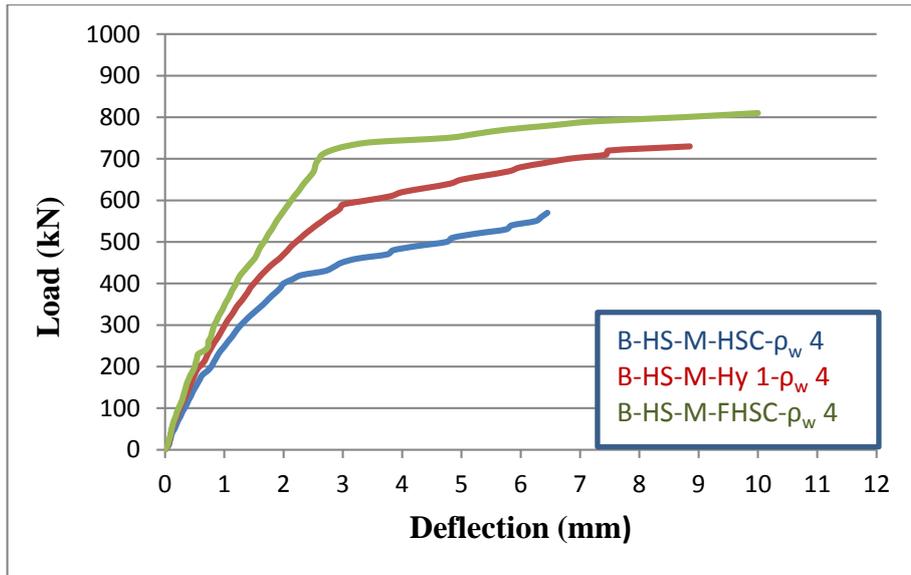


Fig. (11). Load-deflection relationship for different type of beam under monotonic loading.

4.5.3. Effect of Web Reinforcement Ratio

Increasing web reinforcement with different amounts contributed in improving the performance of beams. Fig. (12) shows the effect of ρ_w on load- deflection response for hybrid beams which are tested under monotonic loading.

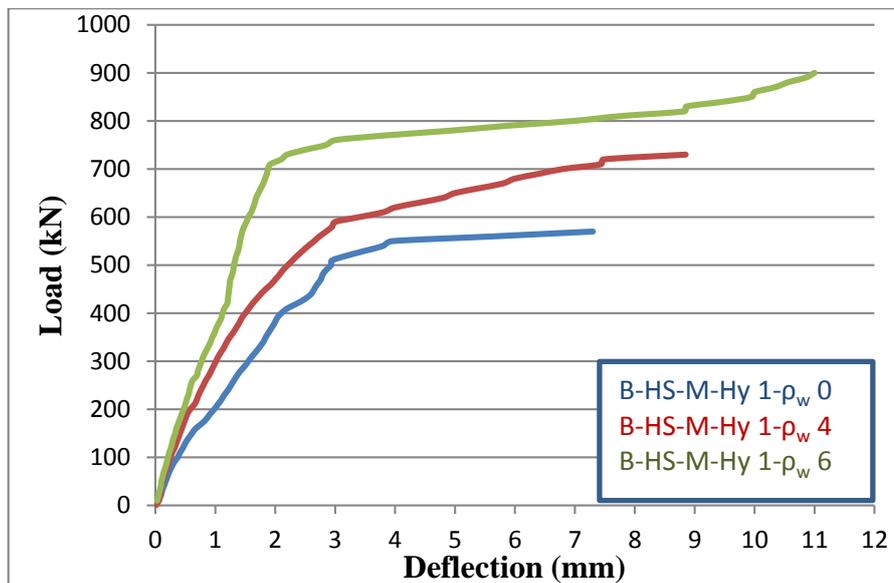


Fig. (12). Load-deflection relationship for hybrid beams with different ρ_w ratios under monotonic loading.

5. ANALYTICAL WORK

Based on the lower-bound theorem, the STM is applied, in which the stress applied to the elements of the STM should not exceed their maximum capacities, and the truss model shall be in equilibrium. When these conditions are met, the truss will exhibit the deformation capacity required by the lower-bound theorem to redistribute the internal stresses and form the arch action [3]. Also, this chapter involves the establishment of the analytical methods that depend on STM techniques for predicting an ultimate load of hybrid HSC deep beams to obtain reasonable and accurate methods of analysis of this type of beams in comparison with available experimental data were analyzed using the following analytical methods:

1. STM according to ACI 318R-14Code [1].
2. Modified STM proposed by Zhang and Tan in March 2007.
3. Modified STM proposed by Zhang and Tan in November 2007.

5.1. Related Work

1. Remodeling buildings often imply a modification of the mechanical behavior of the structural system, which may include the application of concentrated loads to beams that before have only been subjected to distributed loads. In the case of reinforced concrete beams, the new condition causes the beam to support a concentrated load in the cracked condition determined by the distributed loads that had been acting in the past. If the concentrated load is applied at or near the mid-span of the beam, consequently, the shear demand reaches its maximum where the shear capacity is low. At and near the mid-span, in fact, the cracks in the tension zone are vertical like the stirrups. Therefore, the truss mechanism provides the shear capacity with a nil contribution, since both the struts and ties are vertical. Fiber-reinforced polymer composites allow these beams to increase their shear strength, up to guaranteeing adequate safety. A method for analyzing the mechanical behavior of beams with vertical cracks, strengthened with FRP reinforcement, subjected to concentrated loads. The method defines the direction of the fibers that the reinforcement has to be composed of and computes the shear strength of the beam [4].

2. A multiscale analytical model that predicts the lifetime of concrete members with externally bonded FRP reinforcement. The lifetime is dictated by the de-bonding of external reinforcement, which takes place within the concrete cover, where micro-cracks (initial flaws) propagate due to the shear stresses that the bond subjects the concrete cover too. The lifetime is estimated from the propagation of such cracks until a critical crack length is eventually reached, which causes the external FRP reinforcement to lose the bond (delayed de-bonding). The model provides a closed form-solution for the life-through estimation of the external reinforcement, which consists of the interaction between bond shear stresses and lifetime (maximum bond shear stress versus delayed time, *i.e.* the ultimate domain). Crack growth is modeled at the mesoscale, where the velocity of the cracks depends on the model stress intensity factor, but not on the microstructure. The model assumes that the carbonation process has reduced the plasticity and cohesion of the concrete cover to zero; thus, the predictions are slightly conservative (lower bound model). Some experimental results on real scale beams are presented to corroborate the theoretical findings. A practical application of the model shows that delayed de-bonding significantly reduces the service life of concrete members with externally bonded FRP reinforcement [5].

3. The investigation relates to flexural concrete members strengthened by means of external reinforcement bonded adhesively onto the surface, in particular, by fiber-reinforced polymeric strips, sheets, or laminates. Investigation specifically devoted to external reinforcement being already in tension under a dead load or a low fraction of live load. The concrete cover exhibits initial flaws, which were unimportant when a member was not externally reinforced, but that may give rise to slow crack propagation up to delayed de-bonding when the member is externally reinforced. This paper presents a model for predicting the delayed de-bonding. The common de-bonding models, including code provisions, focus mainly on the structural and material scales, and thus ignore delayed failure. On the contrary, this new model focusses on the mesoscale, which considers the velocity of crack growth that leads to de-bonding. While on the nanoscale and microscale, the crack velocity depends on the microstructure. On the mesoscale, the crack velocity depends on the interfacial bond shear stresses and crack length. This dependence can be synthesized by the ratio between the two models. The model describes the delayed de-bonding in terms of interaction between bond shear stress and time (ultimate domain maximum bond shear stress versus delayed time) [6].

5.2. Elements of STM

STM in deep beams is represented by a structural truss. Each type of the elements in an STM serves a unique purpose but must act in conformity to describe accurately the behavior of a structure.

STM consists of the following members and parts:

5.2.1. Struts

Struts are the compression members in the STM. Compression struts fulfill two functions in the STM [1].

1. They serve as the compression zone of the truss which resists moment (prismatic strut).

2. They serve as the diagonal struts which transfer shear to the supports (bottle-shaped strut). Fig. (13) illustrates bottle-shaped, prismatic, and idealized prismatic struts found in a typical STM [10].

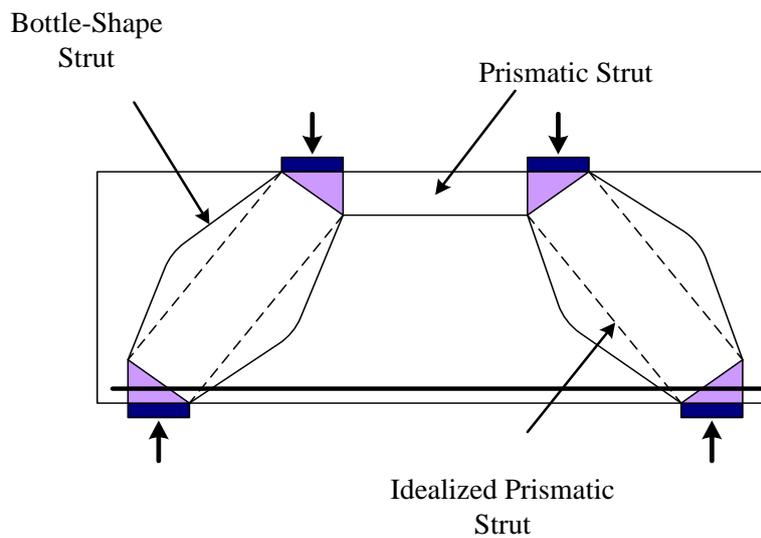


Fig. (13). Strut and Tie Model containing prismatic and bottle-shaped struts.

5.2.2. Ties

Ties are the tension members in the STM, which can be expressed as a reinforcing steel bar. The reinforcement must be dispersed so that its centroid conforms with the tie location. Details like distribution spacing, bar and anchorage are factors that justify the most consideration when placing the reinforcement and selecting [7].

5.2.3. Nodes

Nodes are locations at which struts and ties converge, in the connections of the STM. For example, the nodal zone where 2 struts and a tie meet is mentioned to as a CCT node (C mentions for compression and T mentions for tension) [7].

6. ANALYTICAL RESULTS

6.1. Capacity of the Tested Beams Using the STM

In the present work, the ultimate load for eight simply supported deep beams which were tested under monotonic loading is calculated according to ACI 318 R-14 Code [1]. The comparison between test results and the expected values of the ultimate load is shown in Table 10. From Table 11, it can be noticed that the STM mentioned in ACI 318R-14 Code underestimates the load capacity of deep beams for some beams and overestimates capacities for the other beams. The mean value (\bar{X}) for the ratio of analytical/test results of ultimate loads (P_{An}/P_{Exp}) is 0.94 where P_{An} refers to ultimate loads obtained using analytical methods and P_{Exp} refers to ultimate loads obtained from experimental test, the standard deviation (SD) is 0.14 and the coefficient of variation (CV) is 0.15.

Table 10. Comparison between experimental ultimate loads and those calculated using STM of ACI 318R-14Code [1].

Beam Designation	ρ_w	Type of Beam	SF (%)	Ultimate Load ($2V_u$) (kN)		% P_{An}/P_{Exp}
				STM ACI 318R-14 Code	Experimental Value	
B-HS-M-FHSC 1- ρ_w 4	0.004 (Min.)	Non-Hybrid (FHSC)	1	694	810	0.86
B-HS-M-Hy 1- ρ_w 4	0.004	Hybrid	1	694	730	0.95
B- HS-M-Hy1- ρ_w 6	0.006 (>Min.)	Hybrid	1	694	900	0.77
B-NS-M-Hy1- ρ_w 4	0.004	Hybrid	1	360	370	0.97

(Table 12) contd.....

Beam Designation	ρ_w	Type of Beam	SF (%)	Ultimate Load($2V_n$) (kN)		% P_{Att}/P_{Exp} .
				STM ACI 318R-14 Code	Experimental Value	
B-HS-M-HSC 0- ρ_w 4	0.004	Non-Hybrid (HSC)	0	699	610	1.14

$X' = 0.94$ SD. = 0.14 CV. = 0.15

6.2. Modified of STM Theory

Zhang and Tan in March (2007) [8], submitted a modified STM for calculation of shear strength of reinforced concrete deep beams based on a previous investigation reported by Tan and Cheng [9]. From the structural analysis for simply supported reinforced concrete beams dependent to symmetric two point loads, it is well known that the ultimate load (P) is equal to twice the shear force at the support as per Eq. (1).

$$P = 2V_n \tag{1}$$

The expression for calculation shear strength V_n according to Zhang and Tan [5], is as follows in Eq. (2)

$$V_n = \frac{1}{\frac{4 \sin\theta_s \cos\theta_s}{A_c f_t} + \frac{\sin\theta_s}{A_{str} f'_c}} \tag{2}$$

where;

V_n : shear strength of deep beams (N).

A_c : is the beam effective cross- sectional area (mm^2), equals to $b_w d_c$.

d_c : effective beam depth (mm).

A_{str} : cross-sectional area of the concrete diagonal strut (mm^2), equal to $w_s b_w$.

w_s : effective width of the inclined strut (mm).

b_w : width of deep beam (mm).

f'_c : combined tensile strength of reinforcement and concrete (MPa).

θ_s : angle between the axis of the strut and the horizontal axis of the member.

It can be noted that the expression is the composite tensile strength included contributions from concrete and reinforcement (web and main bars), in Eq. (3)

$$f_t = f_{ct} + f_{st} \tag{3}$$

where; f_{ct} : represents the contribution of concrete tensile strength. f_{st} : represents the contribution of steel reinforcement which consists of two parts, f_{sw} from the web reinforcement and f_{ss} from the longitudinal reinforcement as explain in Eq (4).

$$f_{st} = f_{sw} + f_{ss} \tag{4}$$

Zhang and Tan submitted that the presence of web reinforcement in the strut restricts the inclined cracks from readily increase to every end of the strut. Eq. (5) shows the tensile contribution of web reinforcement at the interface of the nodal zone.

$$f_{sw} = \frac{A_{sw} f_{yw} \sin(\theta_s + \theta_w)}{A_c / \sin\theta_s} \tag{5}$$

For conformity cases of vertical and horizontal web reinforcement, Eq. (6) is reduced to:

$$f_{sw} = \frac{A_{sv} f_{yv} \sin 2\theta_s}{2A_c} + \frac{A_{sh} f_{yh} \sin^2 \theta_s}{A_c} \tag{6}$$

Where:

A_{sv} : total areas of vertical web reinforcement within the shear span (mm^2).

A_{sh} : total areas of horizontal web reinforcement within the shear span (mm^2).

f_{sh} : tensile yield strength of vertical web reinforcement (MPa).

f_{yh} : tensile yield strength of horizontal web reinforcement (MPa).

θ_s : angle between the axis of the strut and the horizontal axis of the member.

θ_w : angle between the web reinforcement and the horizontal axis of beams at the intersection of the reinforcement and the diagonal strut.

The expression f_{ss} refers to the contribution of bottom longitudinal steel, it can be obtained according to the following Eq. (7):

$$f_{ss} = \frac{4A_s f_y \sin \theta_s}{A_c / \sin \theta_s} \tag{7}$$

Where:

A_s : total areas of bottom longitudinal main reinforcement (mm^2).

f_y : tensile yield strength of main reinforcement (MPa).

Table 11 summarized the strength of the deep beams of the present investigation.

Table 11. Comparison between experimental ultimate loads and those calculated using modified STM theory by N. Zhang and K.H. Tan.

Beam Designation	ρ_w	Type of Beam	SF (%)	Ultimate Load ($2V_n$) (kN)		% P_{An}/P_{Exp}
				Modified STM by Zhang and Tan	Experimental Value	
B-HS-M-FHSC 1- ρ_w 4	0.004	Non-Hybrid (FHSC)	1	833	810	1.03
B-HS-M-Hy 1- ρ_w 4	0.004	Hybrid	1	823	730	1.13
B-HS-M-Hy 1- ρ_w 6	0.006	Hybrid	1	851	900	0.95
B-NC-M-Hy 1- ρ_w 4	0.004	Hybrid	1	656	370	1.77
B-HS-M-HSC 0- ρ_w 4	0.004	Non-Hybrid (HSC)	0	796	610	1.3

$X'=1.24$ $SD=0.33$ $CV=0.27$.

From the results, it can be seen overrates ultimate loads compared to test results expect B- HS-M-Hy 1- ρ_w 6 which was cast with ρ_w more than the minimum value (0.006) gives ultimate load in experimental higher than modified. The expression gives capacities which are convergent to experimental values for non-hybrid (FHSC) deep beam B-HS-M-FHSC 1- ρ_w 4 with SF ratio of 1%. The X' for P_{An}/P_{Exp} ratio is 1.24, S.D. is 0.33 and the C.O.V. is 0.27. These results are shown in Fig. (13).

6.3. Size Effect on the Capacity of Deep Beams Using the STM

To investigate the size effect on shear strength of reinforced concrete deep beams, Zhang and Tan in November (2007) [10], carried out an experimental program consisting of three groups of 11 specimens, they noticed that increasing deep beams depth led to decrease in shear strength. They stated that the causes of size effect in deep beams need development, so they submitted that the size effect is influenced by strut geometry and boundary conditions. Zhang and Tan submitted the following modification to Eq. (8) for ultimate shear strength, taking into account the size effect.

$$V_n = \frac{1}{\frac{4 \sin \theta_s \cos \theta_s}{A_c f_t} + \frac{\sin \theta_s}{v A_{str} f_c}} \tag{8}$$

The term v refers to the efficiency factor accounts for the effect of strut geometry, and the effect of strut boundary conditions influenced by web reinforcement. The term v is expressed as follows in Eq. (9)

$$v = \xi \times \zeta \tag{9}$$

where;

ξ : efficiency factor for the effect of strut geometry.

ζ : efficiency factor for the effect of strut boundary conditions influenced by web reinforcement. These parameters are expressed as follows in Eq. (10 and 11)

$$\xi = 0.8 + \frac{0.4}{\sqrt{1+(l-w_s)/50}} \tag{10}$$

$$\zeta = 0.5 + \sqrt{k d_s/l_s} \leq 1.2 \tag{11}$$

Where,

l : length of strut in mm, as shown in Fig. (14).

d_s : diameter of web steel bar, when web steel is not provided, d_s is taken as the minimum diameter of bottom longitudinal steel bars.

l_s : maximum spacing of web steel intercepted by the inclined strut, when web steel is not provided, l_s is equal to l .

$k = 0.5 \times \sqrt{\pi f_y/f_{ct}}$ is a material factor, when web steel is not provided, it is taken as half of the above value.

Table 12 summarized the strength of some deep beams of the present investigation which were tested under monotonic loading.

Table 12. Comparison between experimental ultimate loads and analytical loads obtained using the modified STM method.

Beam Designation	ρ_w	Type of Beam	SF (%)	Ultimate Load(2V _n) (kN)		% P _{An} /P _{Exp.}
				Modified STM Zhang and Tan Article (5.7)	Experimental Value	
B-HS-M-FHSC 1- ρ_w 4	0.004	Non-Hybrid (FHSC)	1	855	810	1.06
B-HS-M-Hy 1- ρ_w 4	0.004	Hybrid	1	845	730	1.16
B- HS-M-Hy 1- ρ_w 6	0.006	Hybrid	1	845	900	0.94
B-NC-M-Hy 1- ρ_w 4	0.004	Hybrid	1	680	370	1.84
B-HS-M-HSC 0- ρ_w 4	0.004	Non-Hybrid (HSC)	0	813	610	1.33

X'=1.29 SD=0.35 CV=0.27.

The modified STM overrate ultimate loads as compared to test results expect B- HS-M-Hy 1- ρ_w 6 gives ultimate load in test result higher than modified STM. The expression gives capacity which is convergent value for non-hybrid (FHSC)deep beam B-HS-M-FHSC 1- ρ_w 4 only. The X' for P_{An}/P_{Exp} ratio is 1.29, SD is 0.35 and the CV is 0.27. These results are shown in Fig. (14).

6.4. Assumptions of Three Methods for Strut and Tie Model Used in the Present Work

1. They assumed that for beams in which bearing and anchorage failures at the nodes are prevented, shear capacity is governed by the compressive capacity of the strut and the mean stress in the strut depends on its dimensions. The strut is assumed to have a uniform width (prismatic strut) defined by geometry of the node at the support.
2. A simple truss model and the resulting failure are resultant of crushing failure of concrete in diagonal strut and tensile failure by splitting of concrete along diagonal strut and yielding of reinforcement.
3. The arch action after the formation of diagonal cracks where it adversely affects the shear strength as the depth becomes larger.

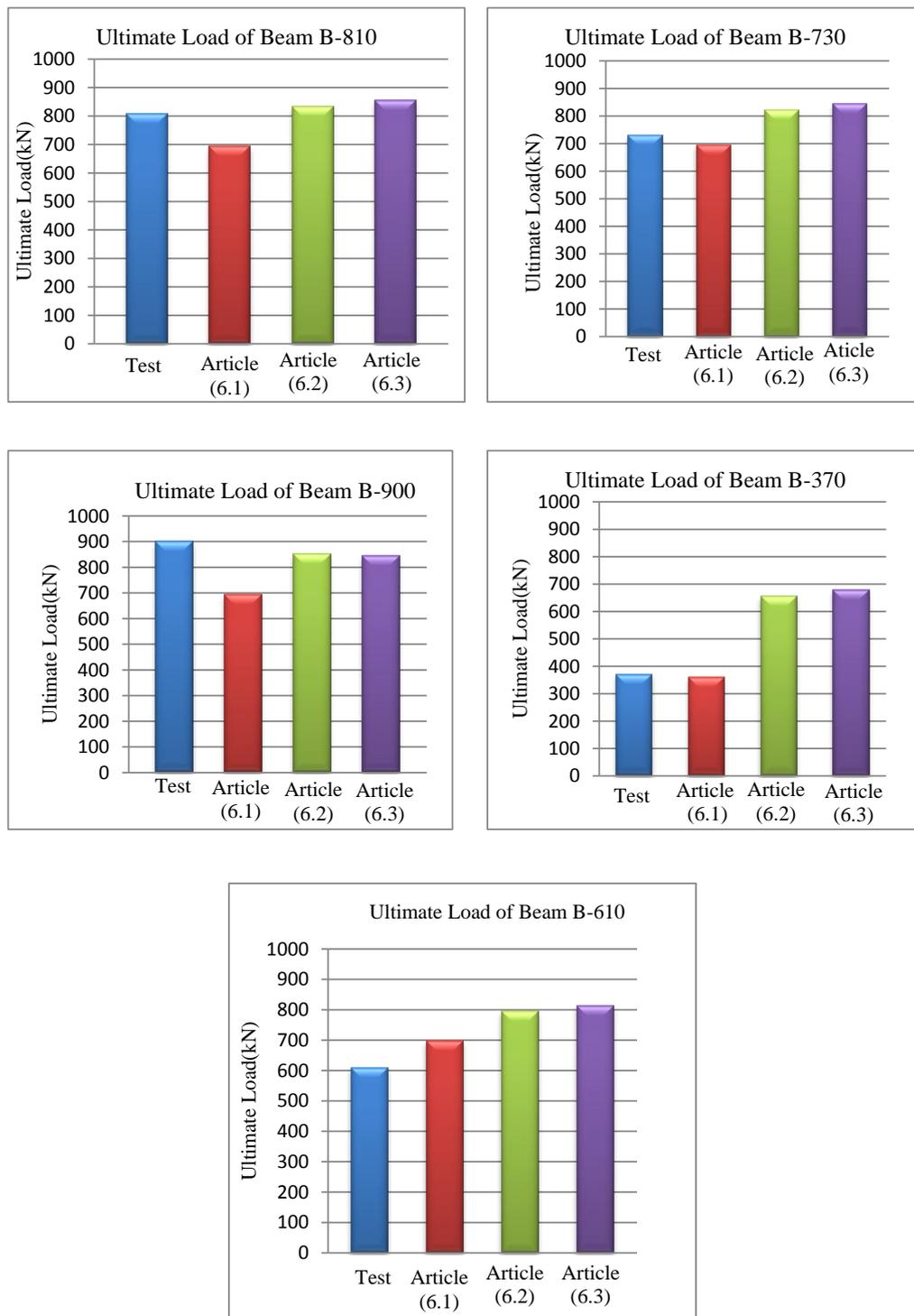


Fig. (14). Comparison between ultimate loads obtained using different experimental and analytical methods.

CONCLUSION

Experimental Stage

In a general manner, the ultimate loads of deep beams subjected to repeated loading (75% of their conforming monotonic loading per cycle) are less than the ultimate loads of conforming beams tested under monotonic loading in the ranges of variables adopted in the present work, as follows:

- a. The decreased percentages in the ultimate load according to repeated loading for non-hybrid deep beams of HSC and FHSC are approximate which are 22.95% and 20.98%, respectively.
 - b. The decreased percentages in the ultimate load according to the repeated loading of hybrid deep beams which have web reinforcement (0.004 and 0.006) as variable are approximate which are 23.97% and 22.22%, respectively.
 - c. The decreased percentage in the ultimate load according to the repeated loading of hybrid deep beams with compressive strength concrete (high and normal) as variable is approximate which are 23.97% and 24.32%, respectively.
 - d. The average value of the decreased percentage of beams subjected to monotonic and 75% repeated loading is 22.17%.
1. The ultimate load of beam increases with existence SF, for beam tested under monotonic load. The increase for beam cast from FHSC (SF 1%) is 32.79% and for the hybrid beam (SF 1% in shear span only), it increases by 19.67% as compared with non- hybrid beam cast from HSCC. The increase in ultimate load of FHSC deep beam is 10.96% as compared with hybrid beam.
 2. It was found that the hybrid beam (SF 1%) in shear span only and non-hybrid beam cast from FHSC (SF 1%) fails under repeated loading in load higher than non-hybrid beam cast from HSC by 18.09% and 36.17%, respectively. While beam which was cast with FC (SF1%) fails in load higher than the hybrid beam by 15.32%.
 3. The ultimate load of HSC of beams tested under monotonic loading is 97.3% for hybrid beam higher than of an identical NSC. Therefore, the concrete compressive strength significantly effects on the capacity of the tested beam. In repeated loading, the increasing of the ultimate load for HSC beam is 98.21% as compared with NSC.
 4. The ultimate load for HSC beams which are tested under monotonic loading increases by 28.07% and 57.89% when the web reinforcement ρ_w increases from (0-0.004) and (0-0.006), respectively. Furthermore, it was noticed that when testing such kind of beams under a repeated loading leads to an increase in the ultimate load from 26.16% to 59.09%, respectively as the ratio of increased from (0-0.004) and from (0-0.006), respectively.

Analytical Stage

1. Results of the ultimate loads of ACI 318R-14 are conservative values as compared to the conforming experimental ones, but it can be noticed that the STM underestimates the load capacity for some beams and overestimates for others. The average amount (X') for the analytical/test ratio of ultimate loads (P_{An}/P_{Exp}) is 0.94, the standard deviation (SD) is 0.14 and the coefficient of variation (CV) is 0.15.
2. The modified STM developed by Zhang and Tan in March 2007 overrates the ultimate loads as compared to test results expect B-HS-M-Hy 1- ρ_w 6 gives in test result higher than modified STM. The X' is 1.24, SD is 0.33 and the CV is 0.27.
3. The modified STM developed by Zhang and Tan in November 2007, that includes the effect of size factor, overrate ultimate loads as compared to test results expect B-HS-M-Hy 1- ρ_w 6 given in test results higher than the modified STM. The X' is 1.29, SD is 0.35 and the CV is 0.27.

CONSENT FOR PUBLICATION

Not applicable.

CONFLICT OF INTEREST

The authors declare no conflict of interest, financial or otherwise.

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Declared none.

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